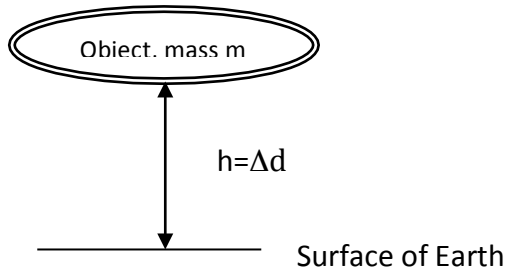


## Energy Continued... (E)

### Gravitational Potential Energy:

- The energy stored in an object due to its distance above the surface of the Earth.
- The energy stored depends on the mass of the object, the height above the surface, and the strength of the gravitational field.
- On Earth, the strength of the gravitational field ( $g$ ) is  $9.8 \text{ m/s}^2$ .
- In this case, an object is raised some height above the surface of the Earth as shown below:



In the example to the left, the object with mass "m" that is acted on by gravity ( $g$ ) is raised a certain distance above the surface of the Earth ( $h$ ). The change in energy of the object is  $\Delta E = mgh$  or

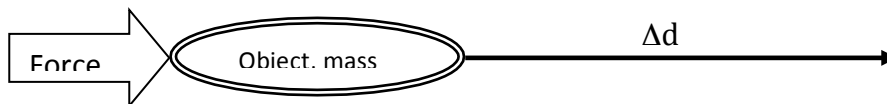
$$E_p = mgh \text{ (if } h_i = 0\text{)}$$

$E_p$  is measured in Joules  
 $m$  is measured in kg  
 $g$  is measured in  $\text{m/s}^2$   
 $h$  is measured in m

**Note:** sometimes in a word problem it is useful to select the lowest height in the problem as a reference point (call that  $h_i = 0$ ) and measure all changes in height (and subsequently changes in energy) in reference to that point. This is called 'relative potential energy' and will simplify calculations.

### Kinetic Energy:

- The energy acquired by an object that experiences a positive change in velocity
- A moving object has energy, and that energy is proportional to the mass and the square of the speed.
- The more mass an object has, and the faster it moves, the more energy it has, and the greater capacity it has to do work.
- In this case, energy is imparted to an object set in motion according to the following:



$$E_k = \frac{1}{2} mv^2$$

$E_k$  is measured in Joules (J);  $m$  is measured in kg;  $v$  is measured in  $\text{m/s}$ .

Name: \_\_\_\_\_ Group: \_\_\_\_\_ Date: \_\_\_\_\_

Name: \_\_\_\_\_

Date: \_\_\_\_\_

### Practice - Kinetic and Potential Energy

1. A crane lifts a 1500 kg car 20 m straight up.
  - a. How much potential energy does the car gain?
  - b. How much energy does the crane transfer to the car?
  - c. How much work does the crane do?
2. A 0.0400 kg rubber ball drops from a height of 5.00 m to the ground and bounces back to a height of 3.00 m above the ground.
  - a. How much potential energy does the ball lose on its trip down?
  - b. How much potential energy does the ball regain on its trip back up?
3. A man on a flying trapeze stands on a platform 20m above the ground, holding the trapeze. The trapeze is 10 m long and is attached to the roof 26m above the surface of the ground. The man swings down, and lets go of the trapeze on the upswing. He has a mass of 60 kg. Calculate his potential energy relative to the ground at the following heights:
  - a. 20 m (on platform)
  - b. 16 m (bottom of swing)
  - c. 18 m (lets go of trapeze)
  - d. 9 m (halfway to ground)
4. What is the kinetic energy of a 0.50 kg ball thrown at 30.0 m/s?
5. What is the mass of an object travelling at 20 m/s with a kinetic energy of 4000 J?
6. What is the speed of a 1.5 kg rock falling with a kinetic energy of 48J?
7. How much work is required to accelerate a 150 kg motorbike from 10 m/s to 20 m/s?
8. A 0.50 kg rubber ball is thrown into the air. At a height of 20 m above the ground, it is travelling at 15 m/s.
  - a. What is the ball's kinetic energy?
  - b. What is its gravitational potential energy relative to the ground?
  - c. How much work has been done by someone at ground level throwing the ball up into the air?

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**Mechanical Energy:**

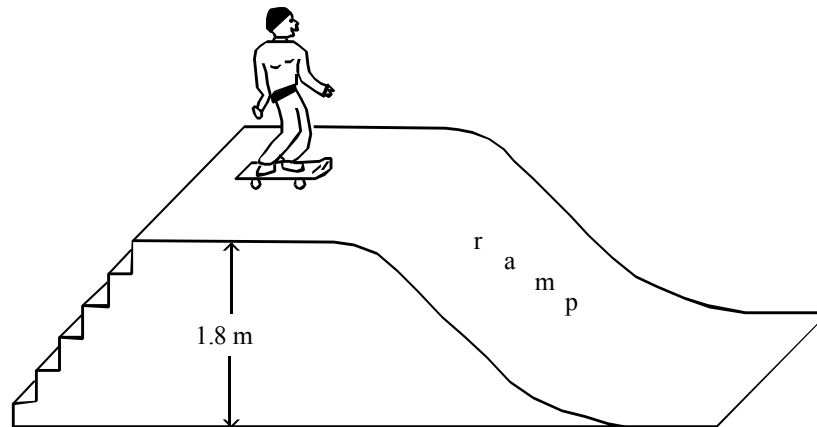
- As we have learned, it is possible to convert between one form of energy and another.
- Specifically we will see that it is possible to change potential energy into kinetic energy and vice versa.
- The sum of the potential energy and kinetic energy possessed by an object is called the mechanical energy.

$$\begin{aligned} E_m &= E_p + E_k \\ &= mgh + \frac{1}{2} mv^2 \end{aligned}$$

- the law of conservation of energy states that in a system without friction, the mechanical energy is always constant.

*Example:*

A child and his skateboard have a mass of 60 kg.  
Starting from rest, he goes down a ramp whose vertical drop is 1.8 m.



What is the boy's speed at the bottom of the ramp? Disregard the effects of friction.

- A) 9.0 m/s
- B) 6.0 m/s
- C) 3.0 m/s
- D) 2.0 m/s

Name: \_\_\_\_\_ Group: \_\_\_\_\_ Date: \_\_\_\_\_

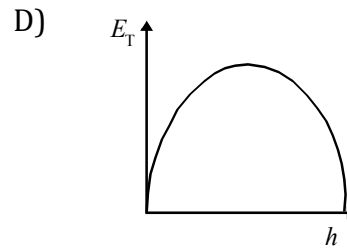
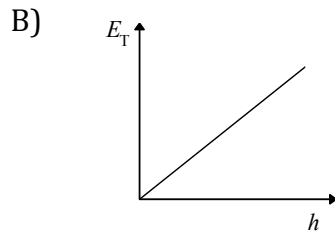
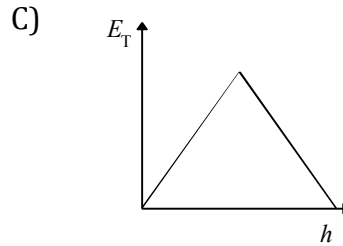
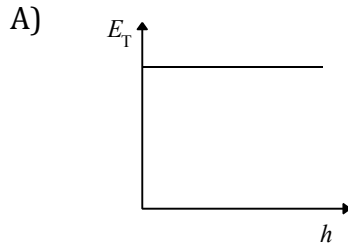
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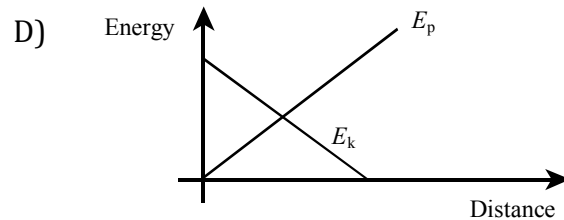
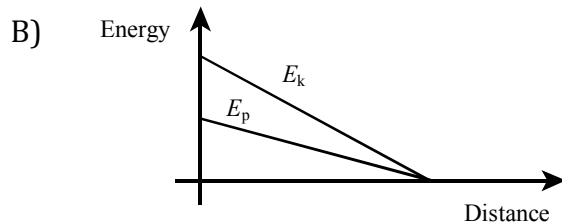
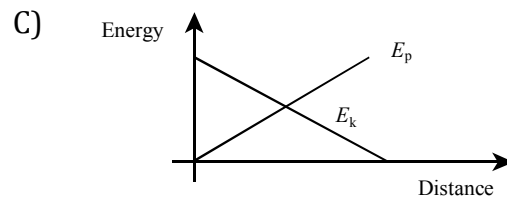
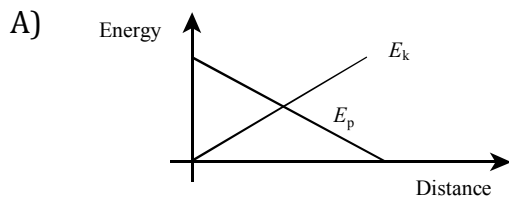
### Practice Questions – Mechanical Energy

1. A football is kicked into the opposing team's zone by the *Dragons'* quarterback.

Which of these graphs shows the **total mechanical energy**,  $E_T$ , of the football as a function of its height,  $h$ ? (Ignore the effects of air resistance.)

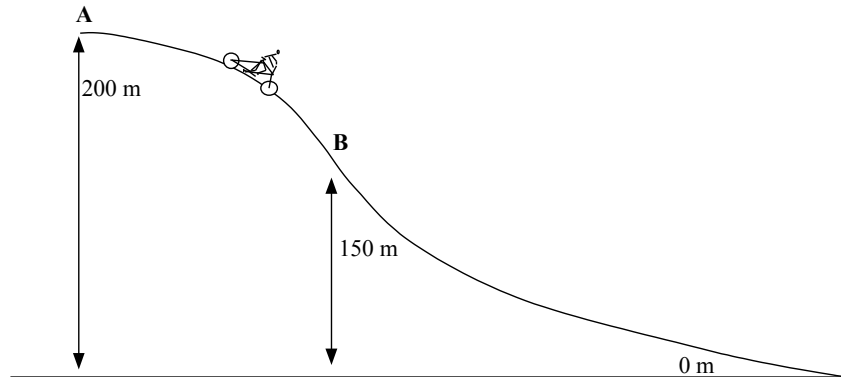


2. A cart is launched up a frictionless inclined plane. Which of the following graphs best represents the transformation of the different types of energy involved in the movement up the ramp?



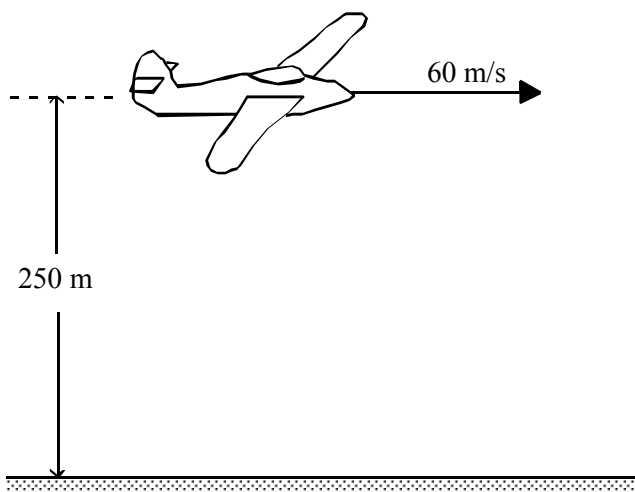
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3. A mountain bike rider starts at rest at point **A**, 200 m above the base of a mountain and descends the slope without pedaling. (Friction is negligible)



What is his velocity at point B, 150 m above the base of the mountain? Show all of your work.

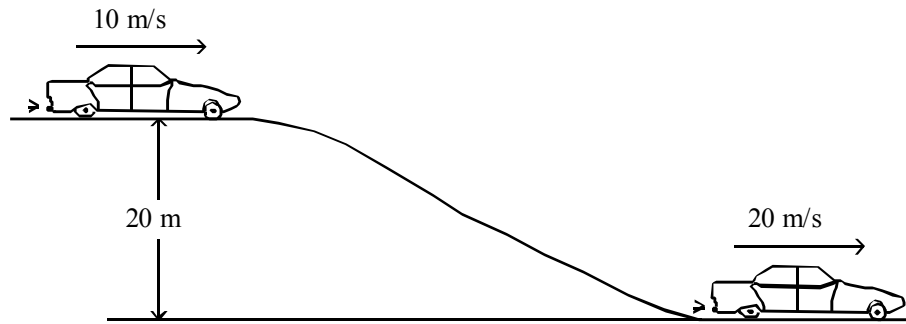
4. A small airplane with a mass of 1000 kg, is flying at 60 m/s at an altitude of 250 m.



What is the total mechanical energy of this airplane with respect to the ground?

Name: \_\_\_\_\_ Group: \_\_\_\_\_ Date: \_\_\_\_\_

5. A car with a mass of 1 000 kg arrives at the top of a hill 20 m high at a speed of 10 m/s. At the bottom of the hill, the speed of the car is 20 m/s.



How much work was done on the car as it went downhill?

- A)  $1.0 \times 10^5$  J  
B)  $1.5 \times 10^5$  J  
C)  $-2.0 \times 10^4$  J  
D)  $-4.6 \times 10^4$  J

6. Calculate the total mechanical energy in each of the following situations?

- A) An automobile of mass 1000 kg travelling in a straight line through a distance of 1000 m at a speed of 30 m/s.  
B) An automobile of mass 1000 kg travelling in a straight line through a distance of 1000 m at a speed of 40 m/s.  
C) A small plane of mass 1000 kg flying at an altitude of 1000 m at a speed of 40 m/s.  
D) A small plane of mass 1000 kg flying at an altitude of 1000 m at a speed of 30 m/s.

7. An Olympic diver runs along a 3 m high diving board, jumps into the air, and dives into the pool below. The 56 kg diver has a speed of 8.0 m/s the moment she leaves the diving board. At what point is her gravitational potential energy at its maximum?

- A) While she is running along the diving board  
B) When she jumps into the air  
C) Just before she hits the water  
D) When she is under water